

MIXED BOUNDARY
VALUE PROBLEMS
OF POTENTIAL THEORY
AND THEIR APPLICATIONS
IN ENGINEERING

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Маѝе, Исааку и Беате посвящается

To Maya, Isaac and Beata

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